



COMPLEX VARIABLES  
SPRING 2011

ASSIGNMENT 10.2  
DUE NOVEMBER 7

**Exercise 1.** What is the largest circle within which the Taylor series at  $z_0 = 0$  for the function  $\tanh z$  converges to  $\tanh z$ ? Find the first two nonzero terms of this series.

**Exercise 2.** Prove that  $\sinh z = \sum_{n=0}^{\infty} \frac{z^{2n+1}}{(2n+1)!}$  for all  $z \in \mathbb{C}$ .

**Exercise 3.** Determine the orders of all of the zeros of  $f(z) = z \sin(z^2)$ .

**Exercise 4.** What is the order of the zero of  $f(z) = e^{z^3} - 1 - z^3$  at the origin?