

Putnam Exam Seminar Fall 2013

Assignment 2 Due September 16

**Exercise 1.** Prove that any positive integer (greater than 1) is either prime or a product of primes.

**Exercise 2.** Consider the sequence  $a_1, a_2, a_3, \ldots$  defined by  $a_1 = 1, a_2 = 2, a_3 = 3$  and  $a_n = a_{n-1} + a_{n-2} + a_{n-3}$  for  $n \ge 4$ . Show that  $a_n < 2^n$  for all  $n \ge 1$ .