

## Introduction to Abstract Mathematics Fall 2013

## Assignment 1.2 Due September 6

**Exercise 1.** Determine the prime constituents of each of the following statements, and use this to express these statements symbolically.

- **a.** If I am tired or hungry, then I cannot study.
- **b.** If it is foggy tonight, then either John must take a taxi or he can't go out.
- **c.** If the Pirates or the Cubs lose and the Giants win, then the Dodgers will be out of first place and, furthermore, I will lose a bet.
- **d.** The sum of two odd integers is even. [*Hint:* This is an implication.]

**Exercise 2.** Let P, Q and R be statements. Construct truth tables for the following compound statements.

- **a.**  $P \rightarrow (Q \lor R)$
- **b.**  $P \rightarrow (Q \land R)$
- c.  $(P \rightarrow Q) \lor R$
- **d.**  $(P \rightarrow Q) \land R$

**Exercise 3.** You visit an island with two types of people: knights (who always tell the truth) and knaves (who always lie). You are approached by two islanders, A and B. Islander A tells you "B is a knight." Islander B then says "A and I are of opposite type." Determine (with justification!) what types A and B are. A truth table may or may not be helpful.