



COMPLEX VARIABLES  
FALL 2024

ASSIGNMENT 4.3  
DUE SEPTEMBER 25

**Exercise 1.** Textbook exercise 1.4.5.

**Exercise 2.** Textbook exercise 1.4.10.

**Exercise 3.** Let  $f(z)$  be a complex-valued function defined on a deleted neighborhood of  $z_0$ . Show that if  $\lim_{z \rightarrow z_0} f(z) = a$ , where  $a \in \mathbb{C}^\times$ , then  $f(z)$  is bounded away from zero on  $D^*(z_0; r)$  for some  $r > 0$ . That is, show there are constants  $M, r > 0$  so that if  $z \in D^*(z_0; r)$ , then  $|f(z)| > M$ .