

Putnam Exam Seminar Fall 2010 Quiz 2 September 15

**Problem 1.** Suppose an arbitrary triangle has interior angles  $\alpha$ ,  $\beta$  and  $\gamma$ . Show that

$$\sin\frac{\alpha}{2}\sin\frac{\beta}{2}\sin\frac{\gamma}{2} \le \frac{1}{4}.$$

**Problem 2.** The area A and an angle  $\theta$  of a triangle are given. Determine the lengths of the sides a and b so that the side opposite  $\theta$  is as short as possible.

**Problem 3.** A convex octagon inscribed in a circle has 4 consecutive sides of length 3 units and 4 consecutive sides of length 2 units. Find its area. Express your answer in the form  $r + s\sqrt{t}$  where r, s, t are natural numbers.