## D

 $\begin{array}{c} {\rm Calculus} \ {\rm I} \\ {\rm Fall} \ 2009 \end{array}$ 

## Exam 2 Practice Problems

**Exercise 1.** A Ferris wheel with a radius of 10 m is rotating at a rate of one revolution every 2 minutes. How fast is a rider rising when his seat is 16 m above ground level?

Exercise 2. Estimate the following quantities.

- **a.**  $\sqrt[3]{0.95}$
- **b.**  $\cos 44^{\circ}$

**Exercise 3.** Find the absolute maximum and minimum values of f on the given interval.

a.  $f(t) = 2\cos t + \sin 2t$ ,  $[0, \pi/2]$ b.  $f(x) = x\sqrt{x - x^2}$ , [0, 1]c.  $f(x) = x^5 - x^3 + 2$ , [-1, 1]

**Exercise 4.** Is there a differentiable function f such that f(0) = -1, f(2) = 4 and  $f'(x) \le 2$  for all x?

**Exercise 5.** Show that the equation  $x^3 - 4x + 1 = 0$  has exactly three real solutions.

**Exercise 6.** Sketch the following curves, indicating all local or absolute maxima and minima, inflection points and asymptotes.

**a.** 
$$y = \sqrt[3]{x^2 - 1}$$
 **b.**  $y = \frac{1}{1 + e^{-x}}$  **c.**  $y = 1 + \frac{1}{x} + \frac{1}{x^2}$ 

Exercise 7. Evaluate the limit.

**a.** 
$$\lim_{x \to 0} \frac{e^{4x} - 1 - 4x}{x^2}$$
 **b.**  $\lim_{x \to 1^+} \left(\frac{x}{x - 1} - \frac{1}{\ln x}\right)$  **c.**  $\lim_{x \to \pi/2^+} (\tan x)^{\cos x}$