

1. Show that the four points  $(1, 1, -1)$ ,  $(0, -2, 6)$ ,  $(-2, 3, -13)$ ,  $(2, 0, 4)$  are coplanar. Find an equation for the plane that contains them.

2. Find a vector  $\mathbf{b}$  perpendicular to  $\mathbf{a} = \langle 1, 3, -2 \rangle$  and a vector  $\mathbf{c}$  perpendicular to both  $\mathbf{a}$  and  $\mathbf{b}$ .

3. The lines

$$L_1 = \begin{cases} x = 4t - 5 \\ y = 5t + 2 \\ z = -4t - 1 \end{cases}, \quad L_2 = \begin{cases} x = -2s - 9 \\ y = -s \\ z = s + 1 \end{cases}$$

intersect each other at exactly one point and therefore lie in a common plane. Find an equation for that plane.

4. Let  $\mathbf{v} = \langle 5, -3, -3 \rangle$  and  $\mathbf{w} = \langle 4, -4, 5 \rangle$ . Compute  $\mathbf{x} = -2\mathbf{v} + 3\mathbf{w}$  and find a unit vector parallel to  $\mathbf{x}$ . Find  $\mathbf{v} \cdot \mathbf{w}$  and  $\mathbf{w} \times \mathbf{v}$ . Are  $\mathbf{v}$  and  $\mathbf{w}$  parallel? Are they perpendicular?

5. Prove the *parallelogram law*: for any pair of vectors  $\mathbf{v}, \mathbf{w}$

$$|\mathbf{v} + \mathbf{w}|^2 + |\mathbf{v} - \mathbf{w}|^2 = 2(|\mathbf{v}|^2 + |\mathbf{w}|^2).$$

[*Hint*: Use the relationship between  $|\cdot|$  and the dot product.]

6. Let

$$\mathbf{A} = \begin{pmatrix} -1 & 4 \\ -1 & 5 \\ 4 & 5 \end{pmatrix} \quad \mathbf{B} = \begin{pmatrix} -4 & 2 \\ -2 & 9 \end{pmatrix} \quad \mathbf{C} = \begin{pmatrix} -4 & 3 & -1 & 3 \\ 1 & -2 & 6 & 7 \end{pmatrix}.$$

Of the six possible products  $\mathbf{AB}$ ,  $\mathbf{BA}$ ,  $\mathbf{AC}$ ,  $\mathbf{CA}$ ,  $\mathbf{BC}$  and  $\mathbf{CB}$ , compute those that are defined.

7. Write the linear system

$$\begin{aligned} 2x - 5y &= 6 \\ 3x + 4y &= -7 \end{aligned}$$

as a matrix equation of the form  $\mathbf{Ax} = \mathbf{b}$ . Find the inverse matrix  $\mathbf{A}^{-1}$  and use it to solve for  $x$  and  $y$ .

8. The solution set to the linear system

$$\begin{aligned} 2x - 3y + 4z &= 1 \\ 3x + 4y - 2z &= 1 \end{aligned}$$

is a line in  $\mathbb{R}^3$ . Find parametric equations for this line.

9. Find the degree 5 Taylor polynomial about  $a = 0$  for

$$f(x) = 2 - x + x^2 + e^x.$$