

**Problem 1.** A tank shaped like a vertical cylinder initially contains water to a depth of 9 ft. A plug on the bottom of the tank is pulled at time  $t = 0$  ( $t$  in hours). After 1 h the depth has dropped to 4 ft. How long will it take all the water to drain from the tank?

**Problem 2.** The shape of a water tank is obtained by revolving the curve  $y = x^{4/3}$  around the  $y$ -axis (units on the coordinate axes are in feet). A plug at the bottom of the tank is removed at 12 noon, when the water depth is 12 ft. At 1 P.M. the water depth is 6 ft. Find the size of the plug and determine at what time the tank will be empty.

**Problem 3.** A 12 hour water clock is to be designed with the shape of the surface obtained by revolving a certain curve  $y = f(x)$  around the  $y$ -axis, subject to the following constraints: its height must be 4 ft, its diameter be 2 ft at that height, and a circular hole must be cut in the bottom so that the water level in the tank falls at the *constant* rate of 4 in./h. Determine the equation the curve must have and also what the radius of the hole in the bottom needs to be.