Math 2326 - Introduction to Abstract Mathematics Assignment 1 - Due Friday, January 18

Problem 1: Which of the following are mathematical statements?

a.
$$a^2 + b^2 = c^2$$
.

b.
$$\int_0^\infty \frac{dx}{x^2}$$

- c. Every even integer is divisible by 4.
- d. 14 is equal to the product of three integers.
- e. πr^2

Problem 2: Let P and Q be statements.

- a. If the statements "P implies Q" and P are both true, what can you conclude about Q?
- b. If the statements "P implies Q" and "not Q" are both true, what can you conclude about P?

Problem 3: Complete the following truth table. What do you notice about the first and last columns?

$$\frac{P \quad \text{not } P \quad \text{not(not } P)}{T}$$

F

Problem 4: Complete the following truth table. What do you notice about the last two columns?

P	Q	not P	P implies Q	(not P) or Q
Т	Τ			
Τ	F			
F	Τ			
F	\mathbf{F}			

Problem 5: Complete the following truth table. What do you notice about the last two columns?

Problem 6: Complete the following truth table. What do you notice about the last two columns?

P	Q	R	P and Q	Q and R	P and $(Q$ and $R)$	(P and Q) and R
Τ	Τ	Τ				
Τ	Τ	F				
Τ	F	Τ				
Τ	F	F				
F	Τ	Τ				
F	Τ	F				
F	F	Τ				
F	F	F				