# Math 2326 - Introduction to Abstract Mathematics Assignment 1 - Due Friday, January 18 

Problem 1: Which of the following are mathematical statements?
a. $a^{2}+b^{2}=c^{2}$.
b. $\quad \int_{0}^{\infty} \frac{d x}{x^{2}}$
c. Every even integer is divisible by 4 .
d. 14 is equal to the product of three integers.
e. $\pi r^{2}$

Problem 2: Let $P$ and $Q$ be statements.
a. If the statements " $P$ implies $Q$ " and $P$ are both true, what can you conclude about $Q$ ?
b. If the statements " $P$ implies $Q$ " and "not $Q$ " are both true, what can you conclude about $P$ ?

Problem 3: Complete the following truth table. What do you notice about the first and last columns?

$$
\begin{array}{lll}
P & \operatorname{not} P & \operatorname{not}(\operatorname{not} P) \\
\hline \mathrm{T} & \\
\mathrm{~F} &
\end{array}
$$

Problem 4: Complete the following truth table. What do you notice about the last two columns?

| $P$ | $Q$ | not $P$ | $P$ implies $Q$ | $($ not $P)$ or $Q$ |
| :--- | :--- | :--- | :--- | :--- |
| T | T |  |  |  |
| T | F |  |  |  |
| F | T |  |  |  |
| F | F |  |  |  |

Problem 5: Complete the following truth table. What do you notice about the last two columns?

| $P$ | $Q$ | $\operatorname{not} P$ | $\operatorname{not} Q$ | $P$ or $Q$ | $\operatorname{not}(P$ or $Q)$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| T | T |  |  |  |  |
| T | F |  |  |  |  |
| F | T |  |  |  |  |
| F | F |  |  |  |  |

Problem 6: Complete the following truth table. What do you notice about the last two columns?

| $P$ | $Q$ | $R$ | $P$ and $Q$ | $Q$ and $R$ | $P$ and $(Q$ and $R) \quad(P$ and $Q)$ and $R$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| T | T | T |  |  |  |
| T | T | F |  |  |  |
| T | F | T |  |  |  |
| T | F | F |  |  |  |
| F | T | T |  |  |  |
| F | T | F |  |  |  |
| F | F | T |  |  |  |
| F | F | F |  |  |  |

