



NUMBER THEORY II  
FALL 2010

ASSIGNMENT 3.2  
DUE SEPTEMBER 15

**Exercise 1.** Let  $m$  and  $n$  be relatively prime integers. Define  $X(a, b) = ab$  and  $Y(d) = (\gcd(d, m), \gcd(d, n))$ .

- a. If  $r, s$  and  $t$  are integers and  $\gcd(r, s) = 1$  prove that  $\gcd(rs, t) = \gcd(r, t) \cdot \gcd(s, t)$
- b. Prove that  $X$  and  $Y$  provide inverse bijections between the sets  $\{a : a|m\} \times \{b : b|n\}$  and  $\{d : d|mn\}$ .

**Exercise 2.** Chapter 2, Exercise 3

**Exercise 3.** Chapter 2, Exercise 27