

**Exercise 1.** Let  $D$  be an integral domain. Prove that if  $p_1, p_2, \dots, p_m, q_1, q_2, \dots, q_n \in D$  ( $m, n \in \mathbb{Z}^+$ ) are primes and  $p_1 p_2 \cdots p_m = q_1 q_2 \cdots q_n$  then  $m = n$  and, after possibly reordering,  $p_i$  and  $q_i$  are associates for  $i = 1, 2, \dots, m$ . [*Suggestion:* Induct on  $m$ .]

**Exercise 2.** Let  $R$  be a ring and let  $I_1 \subset I_2 \subset I_3 \subset \cdots$  be an ascending chain of ideals in  $R$  and let

$$I = \bigcup_{j=1}^{\infty} I_j.$$

- a. Prove that  $I$  is an ideal in  $R$ .
- b. If  $R$  has an identity and each  $I_j$  is proper, prove that  $I$  is also proper.

**Exercise 3.** Page 335, # 38

**Exercise 4.** Page 340, # 24