Exercise 1. Prove that

$$\sum_{n \leq x} \frac{\Lambda(n)}{n} = \int_1^x \frac{\psi(t)}{t^2}\, dt + O(1).$$

Use this to conclude that

$$\int_1^x \frac{\psi(t)}{t^2}\, dt = \log x + O(1).$$