(a) Find the general solution to the given partial differential equation and (b) use it to find the solution satisfying the given initial data.

Exercise 1. $2\dfrac{\partial u}{\partial x} - \dfrac{\partial u}{\partial y} = (x + y)u$

$u(x, x) = e^{-x^2}$

Exercise 2. $\dfrac{\partial u}{\partial x} = -(2x + y)\dfrac{\partial u}{\partial y}$

$u(0, y) = 1 + y^2$

Exercise 3. $y\dfrac{\partial u}{\partial x} + x\dfrac{\partial u}{\partial y} = 0$

$u(x, 0) = x^4$

Exercise 4. $\dfrac{\partial u}{\partial x} + 2y\dfrac{\partial u}{\partial y} = e^{-x} - u$

$u(0, y) = \arctan y$

Exercise 5. $\dfrac{\partial u}{\partial x} + v\dfrac{\partial u}{\partial y} = -ru$ (here r and $v \neq 0$ are constants)

$u(x, 0) = \dfrac{\sin x}{x}$