

Introduction to Abstract Mathematics Spring 2017

Assignment 1.2 Due January 20

Exercise 1. Determine the prime constituents of each of the following statements, and use them to express these statements symbolically.

- **a.** If I am tired or hungry, then I cannot study.
- **b.** If it is foggy tonight, then either John must take a taxi or he can't go out.
- **c.** If the Pirates or the Cubs lose and the Giants win, then the Dodgers will be out of first place and, furthermore, I will lose a bet.
- **d.** The sum of two odd integers is even. [*Hint:* This is an implication.]

Exercise 2. Let P, Q and R be statements. Construct truth tables for the following compound statements.

- **a.** $P \Rightarrow (Q \lor R)$
- **b.** $P \Rightarrow (Q \land R)$
- c. $(P \Rightarrow Q) \lor R$
- **d.** $(P \Rightarrow Q) \land R$

Exercise 3. You visit an island with two types of people: knights (who always tell the truth) and knaves (who always lie). You are approached by two islanders, A and B. Islander A tells you "B is a knight." Islander B then says "A and I are of opposite type." Determine (with justification!) what types A and B are. A truth table may or may not be helpful.

Exercise 4. Textbook exercise 1.5.4.