

## Introduction to Abstract Mathematics Spring 2017

## Assignment 4.2 Due February 10

**Exercise 1.** Let x and y be real numbers. Use the hint of exercise 6.1.12 to prove that

$$x^{n} - y^{n} = (x - y) \sum_{k=0}^{n-1} x^{n-k-1} y^{k} = (x - y)(x^{n-1} + x^{n-2}y + \dots + xy^{n-2} + y^{n-1})$$

for all  $n \in \mathbb{N}$ .

**Exercise 2.** Let  $F_n$  denote the *n*th Fibonacci number (where, as in class, we set  $F_0 = 0$  and  $F_1 = 1$ ). Prove that for all  $n \ge 0$ ,

$$F_n = \frac{1}{\sqrt{5}} \left( \left( \frac{1+\sqrt{5}}{2} \right)^n - \left( \frac{1-\sqrt{5}}{2} \right)^n \right).$$

Exercise 3. Textbook exercise 6.1.7.

**Exercise 4.** Textbook exercise 6.2.12. [Suggestion: See Example 6.2.4.]