



**Instructions:** (a) Find the general solution to the given partial differential equation and (b) use it to find the solution satisfying the given initial data.

**Exercise 1.**  $2\frac{\partial u}{\partial x} - \frac{\partial u}{\partial y} = (x + y)u$   
 $u(x, x) = e^{-x^2}$

**Exercise 2.**  $\frac{\partial u}{\partial x} = -(2x + y)\frac{\partial u}{\partial y}$   
 $u(0, y) = 1 + y^2$

**Exercise 3.**  $y\frac{\partial u}{\partial x} + x\frac{\partial u}{\partial y} = 0$   
 $u(x, 0) = x^4$

**Exercise 4.**  $\frac{\partial u}{\partial x} + 2y\frac{\partial u}{\partial y} = e^{-x} - u$   
 $u(0, y) = \arctan y$

**Exercise 5.**  $\frac{\partial u}{\partial x} + v\frac{\partial u}{\partial y} = -ru$  (here  $r$  and  $v \neq 0$  are constants)  
 $u(x, 0) = \frac{\sin x}{x}$