Modern Algebra
Assignment 12.1
Spring 2019
Due May 1

Exercise 1. Given $n \in \mathbb{N}$ at least 3, let $\zeta_{n}=\cos (2 \pi i / n)+i \sin (2 \pi i / n)=e^{\frac{2 \pi i}{n}}$. Define $R, F \in \operatorname{Perm}(\mathbb{C})$ by $R(z)=\zeta_{n} z$ and $F(z)=\bar{z}$. Prove that the subgroup $\langle R, F\rangle$ of $\operatorname{Perm}(\mathbb{C})$ is isomorphic to $D_{n}$.

Exercise 2. Find all normal subgroups of $D_{n}$.

Exercise 3. Regular polygons are not the only geometric objects with symmetry groups. Determine the symmetry group of the regular tetrahedron.

