



INTRO TO ABSTRACT MATHEMATICS  
SPRING 2020

ASSIGNMENT 9.1  
DUE APRIL 8

**Exercise 1.** Use the division algorithm to (finally!) prove that  $n \in \mathbb{Z}$  is odd if and only if  $n = 2k + 1$  for some  $k \in \mathbb{Z}$ . [*Suggestion:* What are the possible remainders after division by 2?]

**Exercise 2.** Let  $a, b \in \mathbb{N}^+$ ,  $d = \gcd(a, b)$ , and write  $a = dm$  and  $b = dn$  for some  $m, n \in \mathbb{N}^+$ . Prove that  $\gcd(m, n) = 1$ . [*Suggestion:* See exercise 7.2.2.]