



COMPLEX VARIABLES
SPRING 2020

ASSIGNMENT 1.2
DUE JANUARY 29

Exercise 1. Textbook exercise I.1(a)-(e).

Exercise 2. Textbook exercise I.1.3.

Exercise 3. Textbook exercise I.1.5.

Exercise 4. Textbook exercise I.1.6.

Exercise 5. Show that every real matrix of the form $\begin{pmatrix} x & -y \\ y & x \end{pmatrix}$ can be factored uniquely in the form $\begin{pmatrix} r & \\ & r \end{pmatrix} \begin{pmatrix} u & -v \\ v & u \end{pmatrix}$, where $r \in \mathbb{R}_0^+$, and $u, v \in \mathbb{R}$ satisfy $u^2 + v^2 = 1$. Use this to derive the polar representation of complex numbers. [*Suggestion:* Take $r = \sqrt{x^2 + y^2}$.]