

$\begin{array}{c} Complex \ Variables \\ Spring \ 2020 \end{array}$

Assignment 3.2 Due February 12

Exercise 1. Prove that $\overline{e^z} = e^{\overline{z}}$ for all $z \in \mathbb{C}$.

Exercise 2. Find every value of $z \in \mathbb{C}$ for which $\overline{e^{iz}} = e^{i\overline{z}}$.

Exercise 3. Prove that $\log zw = \log z + \log w$, in the sense that both sides take on the same values, for all $z, w \in \mathbb{C}^{\times}$.

Exercise 4. Give necessary and sufficient conditions on $z, w \in \mathbb{C}^{\times}$ so that Log zw = Log z + Log w.