

# Supplement to *Methods for Solving the $p$ -Median Problem: An Annotated Bibliography*

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This is a supplement to *Methods for Solving the  $p$ -Median Problem: An Annotated Bibliography* that contains references to all of the papers considered for that work. The papers referenced here either 1) were included in the annotated bibliography, 2) did not fit the criteria of inclusion, or 3) could not be obtained.

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